Forbearance vs. Interest Rates:
Experimental Tests of Liquidity and Strategic Default Triggers

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## Motivation

What triggers default on debt obligations, and what debt relief policy best prevents it?

- Policymaking-guides design and targeting of relief policies.
- Finance-distinguishes models that emphasize solvency, liquidity, and strategic behavior.
- Macroeconomics-disciplines channels and sizes of effects of fiscal and monetary policies.


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This paper:

- Large-scale $(N=20,944)$ experiment analyzed using the language and framework of an RCT.
- Unique 2-by-2-by-2 design-3 randomized instruments

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- Use transparent event studies to analyze the effects of policies on defaults.
- Test default models emphasizing liquidity and strategic behavior

$$
\text { Decision to Default }=\phi \underbrace{\text { Current Payments }}_{\text {Liquidity }}+\psi \underbrace{\text { PV of Future Payments }}_{\text {Strategic }}+\underbrace{\text { Other Factors }}_{\text {solvency, risk, costs }}
$$

## Preview of Results

## 1. Solvency-face value $F V$ too high

- No! Modifications orthogonal to face value (and income, risk, costs) do affect whether/when to default.
- Rate reductions have immediate effects that persist. Forbearance has no effects beyond expiration.


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2. Liquidity-current payments Pay too high

- A dollar reduction in payments has the same effect through forbearance or interest rates?
- No! Rate reductions reduce payments the least but reduce defaults the most.

$$
\text { by Rate }\left(\mathbb{Z}_{i}^{R}\right)
$$

by Term $\left(\mathbb{Z}_{i}^{T}\right)$

by Forbearance $\left(\mathbb{Z}_{i}^{F}\right)$

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- Whether merely postponing forbearance is effective and defaults are strategic is tightly linked to balance sheets-distress, precaution, assets.


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## 4. Endogenous-heterogenous

- Whether merely postponing forbearance is effective and defaults are strategic is tightly linked to balance sheets-distress, precaution, assets.
- Characterize a strategic trigger whose location is influenced by distress, precaution, and assets.
- Rate reductions have effects beyond liquidity; more powerful for unconstrained.


## Conceptual Framework

Institutional Details

## Experimental Design

Results
Solvency Triggers
Liquidity Triggers
Strategic Triggers
Endogenous Triggers

## Conceptual Framework

## Effect on Payments

$$
\begin{align*}
\text { Payment } & =F V\left(\frac{1}{T}+\frac{R}{2}+\frac{R}{2 T}+\frac{R^{2} T}{12}-\frac{R^{2}}{12 T}+O\left(R^{3}\right)\right) \\
\text { Pay } & \simeq\left(\frac{1}{T}+\frac{R}{2}\right) \tag{1}
\end{align*}
$$

Pay very sensitive to forbearance, much less on the interest rate.

- Typical $R 16 \%$ APR. The typical $T 3$ years. Quarterly Pay of $\frac{1}{12}+\frac{4 \%}{2} \simeq 0.1$.
- Forbearance, postponing amortizing principal, reduces Pay $60 \%$, to quarterly $R$ of $4 \%$.
- $4 p$ APR reduction ( $25 \%$ reduction) reduces Pay $5 \%$.
- $10 \%$ increase in $T^{\prime}$ (off a base of 3 years) reduces Pay $8 \%$.


## Effect on Present Value of Future Payments

$$
\begin{align*}
\text { Present Value }_{0} & =\text { Payment }\left(T-\frac{R^{*} T}{2}-\frac{R^{*} T^{2}}{2}+O\left(R^{* 2}\right)\right) \\
P V_{0} & \simeq\left(1+\left(R-R^{*}\right) \frac{T+1}{2}\right) \tag{2}
\end{align*}
$$

- Rate reductions revalue-alter PV despite keeping FV constant.
- $\Delta R$ of $4 p p$ APR equivalent in $P V$ to a write down of $\frac{1}{2} \cdot T \cdot \Delta R=6 \%$ of $F V$
- To a first-order approximation, the change in $P V$ is independent of $R^{*}$.
- Effects on future Pay account for more or less the entire impact.
- Reduction in Pay stream could exactly be replicated in $P V$ terms via a $F V$ write down.
- Unlike a write-down, borrowers cannot capitalize by prepaying or calling at $F V$.
- Revaluation proportional for Pay and PV, hence larger if debt has a high duration, i.e., $T$ is large.
- Term extensions spread out payments further over time.
- Change in $P V$ proportional to $\frac{1}{2} \cdot T \cdot\left(R-R^{*}\right)$.


## Current Payments and Present Value of Future Payments

Pay ${ }_{1}$ by Rate
Quarterly Payments Normalized by $F V_{0}$

$P V^{f u}{ }_{1}$ by Rate
Present Value of Future Payments Normalized by FVo


## Competing Models

- Solvency: default if the face value too high.
- No credit constraints and $R^{*}=R$.
- Liquidity: default if current payments are too high.
- Affordability constraint, extreme myopia/short-effective planning horizons, or rule-of-thumb behavior.
- Strategic: default by solvent and liquid: if future payments are too high.
- Endogenous: whether defaults are strategic is linked to borrower balance sheets

| Model | What triggers default? |  |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :--- | :--- |
|  | $F V$ | Way | $P V^{f u}$ | $R \downarrow$ | $T \uparrow$ | $F$ |  | Policy |
| Solvency | $\checkmark$ |  |  |  |  |  |  | Write-down |
| Liquidity |  | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | Forbearance |  |
| Strategic |  |  | $\checkmark$ | $\checkmark$ |  |  | Rate reduction |  |
| Endogenous | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | Heterogeneous |  |

Institutional Details

## Macroeconomic and Institutional Details

- Macroeconomic conditions neither depression nor the transitory type.
- Banks or the government are not immediately culpable.
- Defaults best characterized as idiosyncratic.
- Unsecured loans with fixed rates, terms up to 72 months, fixed nominal payments.
- $40 \%$ total, two-thirds of non-mortgage FV outstanding to households.
- No bankruptcy protection.
- 30+ followed up via phone. 90+ forwarded to collections and reported to the credit bureau.
- Wage garnishment up to $25 \%$ of income. Seizure of cash, durables, real estate.
- At the onset, $5 \%$ of aggregate FV in non-performing status.
- Lenders have the capability to facilitate modifications.


## Summary Statistics

|  | Unit | $N$ | mean | s.d. | p10 | p50 | p90 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Demographics |  |  |  |  |  |  |  |
| Age | Years | 20,944 | 38.0 | 9.8 | 26 | 37 | 52 |
| Metro area (1m+) |  | 20,944 | 0.23 | 0.42 | 0 | 0 | 1 |
| Delinquent loan |  |  |  |  |  |  |  |
| Loans (Consolidated) | Count | 20,944 | 1.25 | 0.53 | 1 | 1 | 2 |
| FV (Original) | TRY | 20,944 | 15,281 | 11,172 | 4,546 | 12,298 | 29,081 |
| FV (Remaining) | TRY | 20,944 | 10,403 | 8,980 | 2,480 | 7,728 | 21,639 |
| R | APR, \% | 20,944 | 16.3 | 1.1 | 14.8 | 16.4 | 17.4 |
| $T$ (Original) | Months | 20,944 | 36.8 | 7.7 | 24 | 36 | 48 |
| $T$ (Remaining) | Months | 20,944 | 23.9 | 11.9 | 10 | 21 | 43 |
| Payment | TRY | 20,944 | 531 | 375 | 176 | 434 | 959 |
| Pay | \% of FV | 20,944 | 6.4 | 3.4 | 3.0 | 5.6 | 11.2 |
| New loan |  |  |  |  |  |  |  |
| $F V_{0}$ | TRY | 20,944 | 10,403 | 8,980 | 2,480 | 7,728 | 21,640 |
| $R^{\prime}$ | APR, \% | 20,944 | 13.0 | 2.6 | 9.6 | 13.2 | 16.5 |
| $T^{\prime}$ | Months | 20,944 | 41.3 | 14.9 | 18 | 48 | 61 |
| Forbearance (Take-up) | \% | 7,308 | 32.8 | 46.9 | 0 | 0 | 100 |
| Payment | TRY | 20,944 | 306 | 255 | 77 | 238 | 617 |
| Pay | \% of FV | 20,944 | 3.3 | 1.6 | 1.5 | 3.0 | 5.6 |
| Balance sheet |  |  |  |  |  |  |  |
| 30+ |  | 20,944 | 0.89 | 0.31 | 0 | 1 | 1 |
| 90+ |  | 20,944 | 0.30 | 0.46 | 0 | 0 | 1 |
| Assets (Checking) | TRY | 18,715 | -1,022 | 1,778 | -2,400 | -792 | 0 |
| Limit (Credit Line) | TRY | 18,112 | 5,163 | 8,169 | 650 | 2,750 | 10,800 |
| Debt (Credit Line) | TRY | 18,112 | 4,173 | 8,252 | 0 | 1,653 | 9,890 |

## Experimental Design

## Experimental Timeline

| $\begin{aligned} & \text { Old Contract } \rightarrow \\ & \text { in Arrears } \\ & \quad(R, T) \end{aligned}$ | Randomization | Refinancing | New Contract |
| :---: | :---: | :---: | :---: |
|  |  |  | $\left(R^{\prime}, T^{\prime}, F\right)$ |
|  | $\mathbb{Z}^{R} \times \mathbb{Z}^{T} \times \mathbb{Z}^{F}$ | $R^{\prime} \mid \mathbb{Z}^{R}$ displayed |  |
|  | (2×2×2=8 groups) | $T^{\text {Offer }} \boldsymbol{T}, \mathbb{Z}^{T}$ offered |  |
| $T^{\prime}$ decided |  |  |  |
| $F \mid \mathbb{Z}^{F}$ offered |  |  |  |
| $F$ decided |  |  |  |

## Selection and Randomization

- Participants are preexisting borrowers who hold an unsecured loan in arrears.
- 8 treatment legs in a 2-by-2-by-2 design.
- Draw three random numbers-to determine rate $(R)$, term $(T)$, forbearance ( $F$ ).
- $\mathbb{Z}_{i}^{k}=1$ —High relief designation if number is above a specific threshold.
- Threshold equals 0.5 for rate and term and 0.65 for forbearance.
- Three randomized instruments for econometric evaluation:

$$
\mathbb{Z}_{i}^{R} \quad \mathbb{Z}_{i}^{T} \quad \mathbb{Z}_{i}^{F}
$$

## Covariate Balance

| $Y_{i}=\sum^{k \in R, T, F} \theta^{k} \mathbb{Z}_{i}^{k}+\varepsilon_{i}$ |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Age <br> Years | Loans Consol. Count | $\begin{aligned} & \text { FV } \\ & \text { Org. } \\ & \text { TRY } \end{aligned}$ | $F V_{0}$ <br> Rem. <br> TRY | $\begin{gathered} R \\ \mathrm{Org} . \\ \mathrm{APR}, \% \end{gathered}$ | $\begin{gathered} T \\ \text { Org. } \\ \text { Months } \end{gathered}$ | $\begin{aligned} & \text { Payment } \\ & \text { Org. } \\ & \text { TRY } \end{aligned}$ | $\begin{aligned} & \text { Pay } \\ & \text { Org. } \\ & \mathrm{Nm} \end{aligned}$ | $\begin{gathered} 30+ \\ \% \end{gathered}$ | $\begin{gathered} 90+ \\ \% \end{gathered}$ |
|  | $\mathbb{Z}^{R}$ | $\begin{aligned} & -0.22 \\ & (0.13) \end{aligned}$ | $\begin{gathered} -0.0002 \\ (0.007) \end{gathered}$ | $\begin{gathered} -22 \\ (155) \end{gathered}$ | $\begin{gathered} 34 \\ (124) \end{gathered}$ | $\begin{aligned} & 0.003 \\ & (0.02) \end{aligned}$ | $\begin{gathered} 0.08 \\ (0.11) \end{gathered}$ | $\begin{aligned} & -1.2 \\ & (5.2) \end{aligned}$ | $\begin{aligned} & -0.08 \\ & (0.05) \end{aligned}$ | $\begin{aligned} & -0.82 \\ & (0.43) \end{aligned}$ | $\begin{gathered} -0.31 \\ (0.64) \end{gathered}$ |
|  | $\mathbb{Z}^{T}$ | $\begin{aligned} & -0.07 \\ & (0.13) \end{aligned}$ | $\begin{gathered} -0.01 \\ (0.007) \end{gathered}$ | $\begin{gathered} -3 \\ (154) \end{gathered}$ | $\begin{gathered} 105 \\ (124) \end{gathered}$ | $\begin{gathered} 0.01 \\ (0.02) \end{gathered}$ | $\begin{gathered} -0.11 \\ (0.11) \end{gathered}$ | $\begin{gathered} 0.4 \\ (5.2) \end{gathered}$ | $\begin{array}{r} -0.05 \\ (0.05) \end{array}$ | $\begin{aligned} & -0.10 \\ & (0.43) \end{aligned}$ | $\begin{gathered} 0.67 \\ (0.64) \end{gathered}$ |
|  | $\mathbb{Z}^{F}$ | $\begin{aligned} & -0.02 \\ & (0.14) \end{aligned}$ | $\begin{aligned} & -0.009 \\ & (0.008) \end{aligned}$ | $\begin{gathered} 172 \\ (162) \end{gathered}$ | $\begin{gathered} 170 \\ (130) \end{gathered}$ | $\begin{aligned} & -0.02 \\ & (0.02) \end{aligned}$ | $\begin{gathered} 0.06 \\ (0.11) \end{gathered}$ | $\begin{gathered} 5.5 \\ (5.4) \end{gathered}$ | $\begin{aligned} & -0.02 \\ & (0.05) \end{aligned}$ | $\begin{gathered} 0.45 \\ (0.45) \end{gathered}$ | $\begin{aligned} & -0.03 \\ & (0.67) \end{aligned}$ |
|  | $\alpha$ | $\begin{gathered} 38.1 \\ (0.13) \end{gathered}$ | $\begin{gathered} 1.26 \\ (0.007) \end{gathered}$ | $\begin{gathered} 15,234 \\ (147) \end{gathered}$ | $\begin{gathered} 10,274 \\ (118) \end{gathered}$ | $\begin{gathered} 16.3 \\ (0.02) \end{gathered}$ | $\begin{gathered} 36.8 \\ (0.10) \end{gathered}$ | $\begin{aligned} & 530 \\ & (4.9) \end{aligned}$ | $\begin{gathered} 6.5 \\ (0.05) \end{gathered}$ | $\begin{gathered} 89.6 \\ (0.41) \end{gathered}$ | $\begin{gathered} 30.3 \\ (0.60) \end{gathered}$ |
|  | $N$ | 20,944 | 20,944 | 20,944 | 20,944 | 20,944 | 20,944 | 20,944 | 20,944 | 20,944 | 20,944 |
| $F$ | $p$ | 0.40 | 0.33 | 0.77 | 0.48 | 0.60 | 0.58 | 0.78 | 0.28 | 0.19 | 0.72 |
| K-S | $\mathbb{Z}^{R}$ | 0.41 | 1 | 0.59 | 0.46 | 0.92 | 0.91 | 0.74 | 0.18 | 0.88 | 1 |
|  | $\mathbb{Z}^{T}$ | 1 | 0.98 | 0.27 | 0.56 | 0.65 | 0.33 | 0.67 | 0.22 | 1 | 0.97 |
|  | $\mathbb{Z}^{F}$ | 0.77 | 1 | 0.20 | 0.11 | 0.94 | 1 | 0.12 | 0.41 | 1 | 1 |

## Covariate Balance: Dynamic Pre-trends








## Assignment of Forbearance, Interest Rates, and Term

Randomized $\mathbb{Z}_{i}^{R}, \mathbb{Z}_{i}^{T}$, and $\mathbb{Z}_{i}^{F}$ determine rate $R^{\prime}$, term offer $T^{\text {offer }}$, and forbearance offer.

- Rate $R^{\prime}<R$, off a market rate lower than $R$.
- $\mathbb{Z}_{i}^{R}=0$ assigned 60 bps, $\mathbb{Z}_{i}^{R}=1540$ bps APR reduction.
- Bounded below by $\underline{R}$.
- Term extension offer, $T^{\text {offer }}>T$.
- Not the final term, but a recommendation-an encouragement. Imperfect compliance.
- Group into grids of 12 . Offer $T^{\text {offer }}$ is $\bar{T}_{k}$ times $150 \%$ to $\mathbb{Z}_{i}^{T}=0$, and $\bar{T}_{k}$ times $200 \%$ to $\mathbb{Z}_{i}^{T}=1$.
- $\mathbb{Z}_{i}^{F}=1$ offered forbearance.
- Postponing the payment of the principal for three months.
- Purely transitory, keeping term constant, backloading.
- In contrast to deferment, borrower responsible for interest that accrues.


## First Stage: Interest Rate

## by Rate $\left(\mathbb{Z}_{i}^{R}\right)$

by Term $\left(\mathbb{Z}_{i}^{T}\right)$
by Forbearance $\left(\mathbb{Z}_{i}^{F}\right)$



$\mathbb{Z}_{i}^{R}=0$ are assigned to 60 bps , and $\mathbb{Z}_{i}^{R}=1$ to 540 bps APR rate reduction.
Unannounced. $F=7,551$.
Not negotiable and cannot be changed. Bounded below by a minimum $\underline{R}$.

## First Stage: Term

## by Rate $\left(\mathbb{Z}_{i}^{R}\right)$

by Term $\left(\mathbb{Z}_{i}^{T}\right)$
by Forbearance $\left(\mathbb{Z}_{i}^{F}\right)$




Randomized term extension offer, $T^{\text {offer }}>T$.
Expected. $F=63$.
As in the wild, the borrower is not constrained in choosing $\mathrm{T}^{\prime}$.

## First Stage: Forbearance

## by Rate $\left(\mathbb{Z}_{i}^{R}\right)$

by Term $\left(\mathbb{Z}_{i}^{T}\right)$
by Forbearance $\left(\mathbb{Z}_{i}^{F}\right)$


$\mathbb{Z}_{i}^{F}=1$ are offered forbearance. One-in-three take-up.
Unannounced. $F=2,216$.
Suspends and postpones the payment of the principal for 3 months, backloads. Not free.

## First Stage: Contract Terms

|  | $R^{\prime}$ <br> APR, \% | $T^{\prime}$ <br> Months | $F^{\prime}$ <br> Take-up, \% | $F^{\prime}\left(\mathbb{Z}^{F}=1\right)$ <br> Take-up, \% |
| :---: | :---: | :---: | :---: | :---: |
| $\mathbb{Z}^{R}$ | -3.81 | 0.43 | 0.59 | 1.66 |
|  | $(0.03)$ | $(0.21)$ | $(0.38)$ | $(1.10)$ |
| $\mathbb{Z}^{T}$ | -0.03 | 2.77 | 0.51 | 1.45 |
|  | $(0.03)$ | $(0.20)$ | $(0.38)$ | $(1.10)$ |
| $\mathbb{Z}^{F}$ | -0.02 | -0.32 | 32.8 |  |
| Cons. | $0.03)$ <br> 15.0 <br> $(0.02)$ | $39.22)$ <br> $(0.19)$ | $-0.40)$ <br> $(0.36)$ | 31.2 <br> $(0.96)$ |
| $N$ | 20,944 | 20,944 | 20,944 | 7,308 |
| $F$ | 7,551 | 63 | 2,216 | 2 |

Results

## Solvency Triggers-Event Study

by Rate $\left(\mathbb{Z}_{i}^{R}\right)$
by Term $\left(\mathbb{Z}_{i}^{T}\right)$
by Forbearance $\left(\mathbb{Z}_{i}^{F}\right)$




Modifications orthogonal to the face value and other determinants of default (e.g., income, wealth, risk, costs of default) effect whether and when to default.

## Solvency Triggers-Intent-to-treat Effects

|  | $Y_{i}=\sum^{k \in R, T, F} \theta^{k} \mathbb{Z}_{i}^{k}+f_{t}+\varepsilon_{i}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Short-run |  |  | Long-run |  |  |
|  | $4 m$ | 5 m | $6 m$ | 9 m | 12 m | 15 m |
| Base | 23\% | 28\% | 32\% | 38\% | 40\% | 40\% |
| $\mathbb{Z}^{R}$ | $\begin{aligned} & -2.78 \\ & (0.58) \end{aligned}$ | $\begin{array}{r} -3.51 \\ (0.62) \end{array}$ | $\begin{aligned} & -3.15 \\ & (0.64) \end{aligned}$ | $\begin{gathered} -2.79 \\ (0.66) \end{gathered}$ | $\begin{aligned} & -1.85 \\ & (0.67) \end{aligned}$ | $\begin{aligned} & -2.13 \\ & (0.67) \end{aligned}$ |
| $\mathbb{Z}^{T}$ | $\begin{aligned} & -0.02 \\ & (0.58) \end{aligned}$ | $\begin{gathered} 0.01 \\ (0.62) \end{gathered}$ | $\begin{aligned} & -0.02 \\ & (0.64) \end{aligned}$ | $\begin{aligned} & -0.13 \\ & (0.66) \end{aligned}$ | $\begin{gathered} -0.54 \\ (0.67) \end{gathered}$ | $\begin{aligned} & -0.82 \\ & (0.67) \end{aligned}$ |
| $\mathbb{Z}^{F}$ | $\begin{aligned} & -2.69 \\ & (0.61) \end{aligned}$ | $\begin{aligned} & -2.37 \\ & (0.65) \end{aligned}$ | $\begin{aligned} & -1.96 \\ & (0.67) \end{aligned}$ | $\begin{gathered} 0.24 \\ (0.70) \end{gathered}$ | $\begin{gathered} 0.56 \\ (0.71) \end{gathered}$ | $\begin{aligned} & -0.35 \\ & (0.70) \end{aligned}$ |
| $\mathbb{P}\left(\theta^{R}=0\right)$ | <0.001 | $<0.001$ | <0.001 | <0.001 | 0.006 | 0.002 |
| $\mathbb{P}\left(\theta^{T}=0\right)$ | 0.98 | 0.99 | 0.98 | 0.85 | 0.42 | 0.22 |
| $\mathbb{P}\left(\theta^{F}=0\right)$ | $<0.001$ | $<0.001$ | 0.004 | 0.73 | 0.43 | 0.62 |

## First Stage Effects on Current and Future Payments

|  | Pay $_{1}$ Current | $\mathrm{Pay}_{2}$ <br> Current | $\begin{aligned} & P V_{u}^{f u} \\ & \text { Future } \end{aligned}$ | $\begin{aligned} & P V_{t}^{f u} \\ & \text { Future } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: |
| $\mathbb{Z}^{R}$ | $\begin{array}{r} -0.96 \\ (0.07) \end{array}$ | $\begin{array}{r} -0.85 \\ (0.06) \end{array}$ | $\begin{aligned} & -6.28 \\ & (0.08) \end{aligned}$ | $\begin{aligned} & -5.74 \\ & (0.12) \end{aligned}$ |
| $\mathbb{Z}^{T}$ | $\begin{aligned} & -0.88 \\ & (0.07) \end{aligned}$ | $\begin{array}{r} 1.01 \\ (0.06) \end{array}$ | $\begin{gathered} 0.49 \\ (0.08) \end{gathered}$ | $\begin{gathered} 1.59 \\ (0.12) \end{gathered}$ |
| $\mathbb{Z}^{F}$ | $\begin{array}{r} -1.92 \\ (0.07) \end{array}$ | $\begin{gathered} 0.29 \\ (0.06) \end{gathered}$ | $\begin{gathered} 1.66 \\ (0.09) \end{gathered}$ | $\begin{gathered} 1.63 \\ (0.13) \end{gathered}$ |
| Cons. | $\begin{gathered} 11.6 \\ (0.06) \end{gathered}$ | $\begin{gathered} 11.8 \\ (0.06) \end{gathered}$ | $\begin{gathered} 92.9 \\ (0.08) \end{gathered}$ | $\begin{gathered} 85.2 \\ (0.12) \end{gathered}$ |
| $N$ | 20,944 | 20,944 | 20,944 | 20,944 |
| $F$ | 401 | 160 | 2,128 | 816 |

All modifications reduce current payments—equivalent to 96 cents, 88 cents, and $\$ 1.92$ for each $\$ 100$ of face value, respectively.

## Liquidity Triggers-Payments (First-stage) vs. Defaults (Intent-to-treat)

## by Rate ( $\mathbb{Z}_{i}^{R}$ )

## by Term $\left(\mathbb{Z}_{i}^{T}\right)$

by Forbearance $\left(\mathbb{Z}_{i}^{F}\right)$


Pay and 90+(F) by Term ( $\mathrm{Z}^{\top}$ )


Pay and 90+(F) by Forb. (Z ${ }^{F}$ )


Forbearance has no effects beyond expiration. Rate reductions have immediate effects that persist. Liquidity not the sole driver-Rate cuts reduce payments the least but reduce delinquencies most.

Decision to Default $=\phi \underbrace{\text { Current Payments }}_{\text {Liquidity }}+\psi \underbrace{\text { PV of Future Payments }}_{\text {Strategic }}+\underbrace{\text { Other Factors }}_{\text {wealth, risk, costs }}$

## Effect of Interest Rates on Current and Future Payments

Pay-Current Payments

Pay ${ }_{1}$ by Rate


$$
P a y \simeq\left(\frac{1}{T}+\frac{R}{2}+\frac{R}{2 T}+\frac{R^{2} T}{12}-\frac{R^{2}}{12 T}+O\left(R^{3}\right)\right)
$$

$P V^{f u}$ —Present Value of Future Payments


$$
P V^{f u} \simeq\left(1+\left(R-R^{*}\right) \frac{T}{2}+O\left(R^{* 2}\right)\right)
$$

Effects on $P V^{f u}$ account for more or less the entire impact of interest rate changes.

## A Naive and Non-parametric Decomposition

Let $\phi$ and $\psi$ denote the sensitivity of defaults to current and future payments.
To obtain an estimate, compare the intent-to-treat and first stage effects of $\mathbb{Z}^{R}$ and $\mathbb{Z}^{F}$ :

$$
\begin{aligned}
& -3.15=-0.96 \quad \phi-6.28 \\
& \underbrace{-1.96}_{\text {ITT }}=\underbrace{-1.92}_{\text {FS on Pay }} \underbrace{\phi}_{1.28}+\underbrace{}_{\text {FS on PV }} \begin{array}{c}
\text { fu } \\
\underbrace{\psi}_{0.31}
\end{array}
\end{aligned}
$$

Bivariate Wald yields 1.28 and 0.31 for $\phi$ and $\psi$.
Defaults triggered by both current and future payments; more sensitive to current payments.

$$
\frac{\psi}{\phi}=0.24
$$

News about a dollar in future equal a 24-cent increase in current payments-a strategic effect.

## Strategic Triggers

|  | Panel A: Sensitivity$Y_{i}=\phi \mathrm{Pay}_{i}+f_{t}+\varepsilon_{i}$ |  |  |  | Panel B: Decomposition$Y_{i}=\phi \mathrm{Pay}_{i}+\psi P V_{i}^{\text {fu }}+f_{t}+\varepsilon_{i}$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} \text { Pay } \\ \text { Current } \end{gathered}$ | $\begin{gathered} 3.31 \\ (0.72) \end{gathered}$ | $\begin{aligned} & -0.007 \\ & (0.74) \end{aligned}$ | $\begin{gathered} 1.03 \\ (0.35) \end{gathered}$ | $\begin{gathered} \text { Pay } \\ \text { Current } \end{gathered}$ | $\begin{gathered} 1.11 \\ (0.29) \end{gathered}$ | $\begin{gathered} 1.29 \\ (0.32) \end{gathered}$ | $\begin{gathered} 1.21 \\ (0.29) \end{gathered}$ | $\begin{gathered} 3.11 \\ (0.80) \end{gathered}$ |
|  |  |  |  | $P V^{f u}$ <br> Future | $\begin{gathered} 0.33 \\ (0.10) \end{gathered}$ | $\begin{gathered} 0.31 \\ (0.10) \end{gathered}$ | $\begin{gathered} 0.36 \\ (0.10) \end{gathered}$ | $\begin{gathered} 0.92 \\ (0.29) \end{gathered}$ |
| Instrument |  |  |  | Instrument |  |  |  |  |
| $\mathbb{Z}^{R}$ | $\checkmark$ |  |  | $\mathbb{Z}^{R}$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| $\mathbb{Z}^{T}$ |  | $\checkmark$ |  | $\mathbb{Z}^{T}$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |
| $\mathbb{Z}^{F}$ |  |  | $\checkmark$ | $\mathbb{Z}^{F}$ | $\checkmark$ | $\checkmark$ |  |  |
| $\mathbb{P}(\phi=0)$ |  |  |  | $\mathbb{P}(\phi=\psi=0)$ | $<0.001$ | $<0.001$ | <0.001 | <0.001 |
|  | $<0.001$ | 0.99 | 0.004 | $\mathbb{P}(\phi=0)$ | $<0.001$ | $<0.001$ | <0.001 | $<0.001$ |
|  |  |  |  | $\mathbb{P}(\psi=0)$ | 0.001 | 0.003 | <0.001 | 0.001 |
|  |  |  |  | $\mathbb{P}(\phi=\psi)$ | 0.017 | 0.007 | $0.008$ | 0.015 |
|  |  |  |  | $\psi / \phi$ | 0.30 | 0.24 | 0.30 | 0.29 |

Forbearance needs to reduce payments by three times to obtain the impact of rate reductions. Identified moment $\psi / \phi$-dollar change in $P V^{f u}$ similar to a 30-cent increase in quarterly Pay.

## Liquidity vs. Strategic Effects of Interest Rates

Total revaluation effect of interest rates—approximately $\frac{1}{2} T \Delta R$
Under perfect intertemporal substitution, more or less the entire impact through future payments.
Nevertheless, refinancing a mortgage is often interpreted as a liquidity shock.


Strategic effects equivalent to a deferral program that reduces monthly payments by $5 \%$ of average monthly household disposable income. $-0.30 \times 6.28 \% \times \frac{10,403}{3,844}$.

## Balance Sheet Effects-Late Payments and Other Accounts

| Panel A: Late Payments |  |  |  |  |  |  |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $0+$ | $30+$ | $120+$ | $150+$ | Panel B: Other |  |
|  | $30+$ | $90+$ |  |  |  |  |
| Base | $58 \%$ | $38 \%$ | $30 \%$ | $30 \%$ | $4 \%$ | $1 \%$ |
| $\mathbb{Z}^{R}$ | -3.58 | -3.53 | -3.00 | -3.17 | -0.11 | -0.01 |
|  | $(0.68)$ | $(0.67)$ | $(0.63)$ | $(0.63)$ | $(0.25)$ | $(0.14)$ |
| $\mathbb{Z}^{F}$ | -3.80 | -3.08 | -1.87 | -1.62 | 0.84 | 0.28 |
|  | $(0.71)$ | $(0.70)$ | $(0.66)$ | $(0.66)$ | $(0.27)$ | $(0.14)$ |
| Pay | 1.81 | 1.69 | 1.07 | 1.00 | -0.26 | -0.09 |
| Current | $(0.31)$ | $(0.31)$ | $(0.29)$ | $(0.29)$ | $(0.12)$ | $(0.06)$ |
| $P V^{f u}$ | 0.29 | 0.30 | 0.31 | 0.35 | 0.06 | 0.02 |
| Future | $(0.11)$ | $(0.11)$ | $(0.10)$ | $(0.10)$ | $(0.04)$ | $(0.02)$ |
| $\mathbb{P}(\psi=0)$ | 0.008 | 0.004 | 0.002 | $<0.001$ | 0.13 | 0.43 |
| $\mathbb{P}(\phi=\psi)$ | $<0.001$ | $<0.001$ | 0.02 | 0.04 | 0.014 | 0.11 |
| $\phi / \psi$ | 0.16 | 0.18 | 0.29 | 0.35 | $<0$ | $<0$ |

Early-cycle more sensitive to forbearance and current payments-i.e., driven by liquidity.
Late-cycle is more sensitive to rate reductions and future payments-i.e., strategic.

## Robustness-Discounting

| $R^{*}$ | Constant |  |  | Hyperbolic |  | Hetero. <br> Old $R_{i}$ | Expected $\mathbb{E}[P V]$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0\% | 24\% | 48\% | $\beta=0.9$ | $\beta=0.8$ |  |  |
| Pay Current | $\begin{gathered} 1.15 \\ (0.29) \end{gathered}$ | $\begin{gathered} 1.10 \\ (0.30) \end{gathered}$ | $\begin{gathered} 1.07 \\ (0.30) \end{gathered}$ | $\begin{gathered} 1.11 \\ (0.29) \end{gathered}$ | $\begin{gathered} 1.11 \\ (0.29) \end{gathered}$ | $\begin{gathered} 1.12 \\ (0.29) \end{gathered}$ | $\begin{gathered} 1.79 \\ (0.33) \end{gathered}$ |
| $\begin{gathered} P V^{f u} \\ \text { Future } \end{gathered}$ | $\begin{gathered} 0.25 \\ (0.07) \end{gathered}$ | $\begin{gathered} 0.35 \\ (0.11) \end{gathered}$ | $\begin{gathered} 0.38 \\ (0.15) \end{gathered}$ | $\begin{gathered} 0.37 \\ (0.11) \end{gathered}$ | $\begin{gathered} 0.41 \\ (0.13) \end{gathered}$ | $\begin{gathered} 0.32 \\ (0.10) \end{gathered}$ | $\begin{gathered} 0.71 \\ (0.22) \end{gathered}$ |
| $\begin{array}{r} \mathbb{P}(\psi=0) \\ \mathbb{P}(\phi=\psi) \\ \psi / \phi \end{array}$ | $\begin{gathered} <0.001 \\ 0.003 \\ 0.22 \end{gathered}$ | $\begin{gathered} 0.002 \\ 0.026 \\ 0.32 \end{gathered}$ | $\begin{gathered} 0.017 \\ 0.078 \\ 0.36 \end{gathered}$ | $\begin{gathered} 0.001 \\ 0.025 \\ 0.33 \end{gathered}$ | $\begin{gathered} 0.001 \\ 0.040 \\ 0.37 \end{gathered}$ | $\begin{gathered} <0.001 \\ 0.015 \\ 0.29 \end{gathered}$ | $\begin{gathered} 0.001 \\ <0.001 \\ 0.40 \end{gathered}$ |

## Endogenous Triggers

Determinants of the shape of default region in models macroeconomists routinely use:

- Distress
- Precaution
- Assets


## Endogenous Triggers-Heterogeneity in Intent-to-treat Effects

|  | Panel A: Distress Days Late |  |  | Panel B: Precaution Times Binding |  |  | Panel C: <br> Assets <br> Checking Balances |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (A1) | (A2) | (A3) | (B1) | (B2) | (B3) | (C1) | (C2) | (C3) |
|  | 90+ | 31-90 | < 30 | $\emptyset$ | High | Low | $\emptyset$ | Low | High |
| Frac. | 0.30 | 0.59 | 0.11 | 0.14 | 0.43 | 0.43 | 0.10 | 0.45 | 0.45 |
| Base | 32\% | 36\% | 11\% | 28\% | 35\% | 29\% | 30\% | 32\% | 32\% |
| $\mathbb{Z}^{R}$ | $\begin{aligned} & -4.72 \\ & (1.16) \end{aligned}$ | $\begin{array}{r} -2.41 \\ (0.86) \end{array}$ | $\begin{array}{r} -1.50 \\ (1.29) \end{array}$ | $\begin{aligned} & -5.43 \\ & (1.68) \end{aligned}$ | $\begin{aligned} & -2.04 \\ & (1.00) \end{aligned}$ | $\begin{array}{r} -3.38 \\ (0.95) \end{array}$ | $\begin{array}{r} -3.27 \\ (1.93) \end{array}$ | $\begin{array}{r} -2.47 \\ (0.96) \end{array}$ | $\begin{array}{r} -3.72 \\ (0.95) \end{array}$ |
| $\mathbb{Z}^{F}$ | $\begin{aligned} & -4.55 \\ & (1.21) \end{aligned}$ | $\begin{aligned} & -1.29 \\ & (0.90) \end{aligned}$ | $\begin{gathered} 0.53 \\ (1.36) \end{gathered}$ | $\begin{aligned} & -3.52 \\ & (1.75) \end{aligned}$ | $\begin{aligned} & -1.74 \\ & (1.05) \end{aligned}$ | $\begin{aligned} & -1.63 \\ & (1.00) \end{aligned}$ | $\begin{aligned} & -3.58 \\ & (2.04) \end{aligned}$ | $\begin{array}{r} -1.89 \\ (1.00) \end{array}$ | $\begin{aligned} & -1.67 \\ & (1.00) \end{aligned}$ |
| $\mathbb{P}\left(\theta^{R}=0\right)$ | $<0.001$ | 0.005 | 0.25 | 0.001 | 0.04 | <0.001 | 0.09 | 0.01 | <0.001 |
| $\mathbb{P}\left(\theta^{F}=0\right)$ | $<0.001$ | 0.15 | 0.70 | 0.045 | 0.10 | 0.10 | 0.08 | 0.06 | 0.10 |

Borrowers not in default do not find forbearance attractive as it only alters the timing of repayment.
Rate reductions are more effective for participants who can intertemporally substitute.

## Endogenous Triggers-Heterogeneity in Treatment Effects

|  | Panel A: Distress Days Late |  |  | Panel B: Precaution Times Binding |  |  | Panel C: <br> Assets <br> Checking Balances |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (A1) | (A2) | (A3) | (B1) | (B2) | (B3) | (C1) | (C2) | (C3) |
|  | 90+ | 31-90 | < 30 | $\emptyset$ | High | Low | $\emptyset$ | Low | High |
| Frac. in Bin | 0.30 | 0.59 | 0.11 | 0.14 | 0.43 | 0.43 | 0.10 | 0.45 | 0.45 |
| Pay Current | $\begin{gathered} 2.40 \\ (0.55) \end{gathered}$ | $\begin{gathered} 0.66 \\ (0.38) \end{gathered}$ | $\begin{gathered} 0.08 \\ (0.70) \end{gathered}$ | $\begin{gathered} 2.19 \\ (0.87) \end{gathered}$ | $\begin{gathered} 0.79 \\ (0.46) \end{gathered}$ | $\begin{gathered} 1.09 \\ (0.42) \end{gathered}$ | $\begin{gathered} 2.08 \\ (0.91) \end{gathered}$ | $\begin{gathered} 1.04 \\ (0.45) \end{gathered}$ | $\begin{gathered} 0.97 \\ (0.43) \end{gathered}$ |
| $P V^{f u}$ <br> Future | $\begin{gathered} 0.39 \\ (0.18) \end{gathered}$ | $\begin{gathered} 0.28 \\ (0.14) \end{gathered}$ | $\begin{gathered} 0.23 \\ (0.22) \end{gathered}$ | $\begin{gathered} 0.43 \\ (0.25) \end{gathered}$ | $\begin{gathered} 0.20 \\ (0.17) \end{gathered}$ | $\begin{gathered} 0.39 \\ (0.15) \end{gathered}$ | $\begin{gathered} 0.19 \\ (0.30) \end{gathered}$ | $\begin{gathered} 0.23 \\ (0.16) \end{gathered}$ | $\begin{gathered} 0.44 \\ (0.15) \end{gathered}$ |
| $\mathbb{P}(\psi=0)$ | <0.001 | 0.08 | 0.91 | 0.012 | 0.08 | 0.009 | 0.02 | 0.02 | 0.02 |
| $\mathbb{P}(\psi=0)$ | 0.03 | 0.04 | 0.29 | 0.078 | 0.22 | 0.01 | 0.53 | 0.15 | 0.003 |
| $\mathbb{P}(\phi=\psi)$ | <0.001 | 0.38 | 0.85 | 0.071 | 0.26 | 0.13 | 0.06 | 0.12 | 0.26 |
| $\psi / \phi$ | 0.16 | 0.43 | 2.88 | 0.20 | 0.26 | 0.35 | 0.09 | 0.22 | 0.45 |
| Strategic | 0.55 | 0.73 | 0.98 | 0.58 | 0.63 | 0.73 | 0.47 | 0.57 | 0.77 |

## Endogenous Triggers-Heterogeneity in Treatment Effects





Distress, precaution, and assets all determine the location of the liquidity trigger.


## Endogenous Triggers-Heterogeneity in Strategic Effects of Interest Rates



For early-cycle delinquencies, $98 \%$ of the effects of interest rates is through strategic channels.

## Concluding Remarks

Debt relief experiment to study default triggers and policy to prevent it.

- Liquidity is not the sole trigger
- Strategic borrowers default in response to changes orthogonal to solvency and liquidity.
- Endogeneity of triggers-whether defaults are strategic is tightly linked to balance sheets.

Characterize single strategic trigger whose location is influenced by distress, precaution, and assets.

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Rate reductions are substantially more powerful for unconstrained borrowers.

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Rate reductions are substantially more powerful for unconstrained borrowers.

In future work, it would be valuable to ask:

- Are commonly used calibrations compatible with the shape of the default region?
- Studying liquidity and strategic effects for nondelinquent refinancing.

Thank you!

